

Using type inference to discover interesting properties about programs: Pointer Analysis

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What is pointer analysis?

- Find out what each pointer could point to
 - For each point in the program (**flow sensitive**)
 - For all points in the program (**flow insensitive**)

- Example:

```
p = &x;
*p = 10;
p = &y;
*p = 20;
```

← p points to x

p points to x or y

← p points to y

Why do we need pointer analysis? (I)

- ```
f(int *p, int *q) {
 *p = E1;
 *q = E2;
 print(*p); }
```
- Accessing memory (e.g., \*p) is expensive:
- ```
f(int *p, int *q) {  
    *p = E1;  
    *q = E2;  
    print(E1); }
```
- When is this legal?

Why do we need pointer analysis (II)

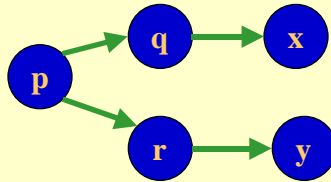
- ```
f(int **p, int **q) {
 *q = NIL;
 **p = E; }
```
- Segmentation violation!!!



Why is \*p NIL???

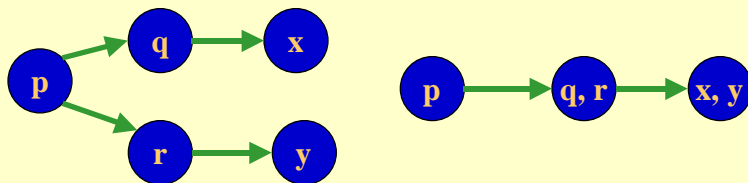
## Storage shape graph

- Describes the shape of storage
  - Nodes represent one or more memory locations
  - Edges represent points-to relationships
- E.g.,  
q = &x;  
r = &y;  
if (cond) p = &q  
else p = &r



## Storage shape graph and approximations

- Steensgaard computes SSGs in which nodes have at most one outgoing edge



## Algorithm approach

- Traditional types specify allowable values
- Paper computes "non-standard" types that specify points-to relationships
- Even traditional types have some points-to information built in  
e.g., variable  $v: T$  and  $u: U$  cannot point to the same object of  $T$  and  $U$  are "incompatible types"

## Paper approach (cont.)

- Give a set of rules that indicate when an expression is **well typed**
- Use rules to perform type inference
- Inferred types make up the storage shape graph

## How does this topic fit into this class?

- The problem is simpler than SML
  - We can see a full type inference system in action
- Idea that different kinds of type systems exist
  - Type system describes properties of programs

## The types

$\alpha ::= \tau \times \lambda$       Types of values  
 $\tau ::= \perp \mid \text{ref}(\alpha)$       Types of locations  
 $\lambda ::= \perp \mid \text{lam}(\alpha_1.. \alpha_n)(\alpha_{n+1}.. \alpha_{n+m})$       Types of functions

In english...

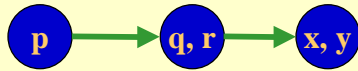
A type is a pair of a  $\tau$  and a  $\lambda$ :

$\tau$  represent pointers to data

$\lambda$  represent pointers to functions

$\perp$  (pronounced bottom) means not yet known to be a pointer

## Example



p:  $\tau_1 = \text{ref}(\tau_2 \times \perp)$  i.e., a pointer to  $\tau_2$

q:  $\tau_2 = \text{ref}(\tau_3 \times \perp)$  i.e., a pointer to  $\tau_3$

r:  $\tau_2$

x:  $\tau_3 = \text{ref}(\perp \times \perp)$  i.e., not known to be a pointer

y:  $\tau_3$

## Typing rules

- Not too different from programming language types

typing requirements

expression

Two ways of thinking about it:

If typing requirements are satisfied then expression is legal

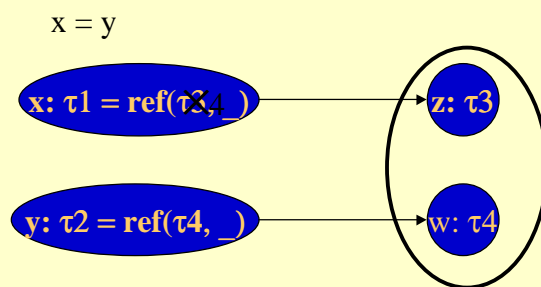
If you see expression then assert that typing requirements must hold

## Simple assignment typing rule

$$\frac{\begin{array}{l} A \vdash x: \text{ref}(\alpha_1) \\ A \vdash y: \text{ref}(\alpha_2) \\ \alpha_2 \leq \alpha_1 \end{array}}{A \vdash \text{welltyped}(x = y)}$$

Type inference view of the rule:  
when you see  $x = y$ , assert that  $\alpha_2 \leq \alpha_1$   
(i.e.,  $\alpha_2$  is bottom or  $\alpha_2 = \alpha_1$ )

## Example



$\tau_3$  and  $\tau_4$  are made equivalent

## Address assignment typing rule

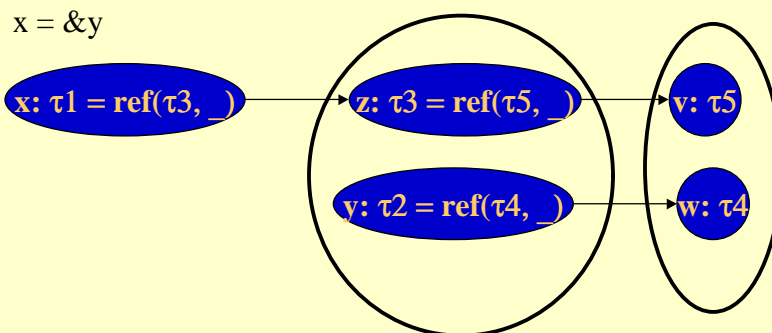
$$\frac{A \vdash x: \text{ref}(\tau \times \_) \quad A \vdash y: \tau}{A \vdash \text{welltyped}(x = \&y)}$$

Type inference view of the rule:

when you see  $x = \&y$ , assert that  $x$  is a pointer to  $\tau$  which is  $y$ 's type

Note: don't need a  $\leq$  requirement since  $\&y$  is a pointer by definition

## Example



$\tau_2$  and  $\tau_3$  are made equivalent  
which causes  $\tau_4$  and  $\tau_5$  to become equivalent

## Dereferenced assignment type rule

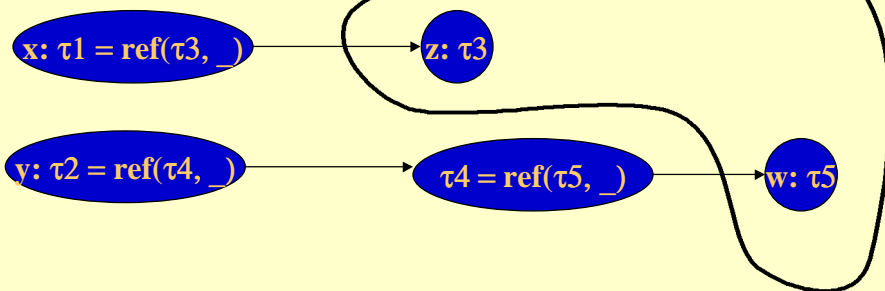
$$\frac{\begin{array}{l} A \vdash x: \text{ref}(\alpha_1) \\ A \vdash y: \text{ref}(\text{ref}(\alpha_2) \times \_) \\ \alpha_2 \leq \alpha_1 \end{array}}{A \vdash \text{welltyped}(x = *y)}$$

Type inference view of the rule:

when you see  $x = *y$ , assert that  $x$  is a pointer to whatever  $*y$  was a pointer to if  $*y$  might be a pointer

## Example

$x = *y$



$\tau_3$  and  $\tau_5$  are made equivalent (assume both are pointers)

## Function pointer assignment rule

$$\begin{array}{l} A \vdash x: \text{ref}(\_ \times \text{lam}(\alpha1)(\alpha2)) \\ A \vdash f: \text{ref}(\alpha1) \\ A \vdash r: \text{ref}(\alpha2) \\ \text{forall } s \text{ in } S^* : A \vdash \text{welltyped}(s) \\ \hline A \vdash \text{welltyped}(x = \text{fun}(f) \rightarrow (r): S^*) \end{array}$$

## Things to note

- Each type “points to” at most one other location
  - => SSG nodes have at most one outgoing edge
  - => Merging two types causes their referent types to also be merged

## Type inference rules

- Type inference rules are derived directly from the typing rules
- Complexity:
  - If a type is  $\perp$  then it should not be merged immediately with other types-causes imprecision
  - Defer merges of  $\perp$ . If it is found to be a pointer, then merge then.

## An example

$$\frac{\begin{array}{l} A \vdash x: \text{ref}(\alpha_1) \\ A \vdash y: \text{ref}(\alpha_2) \\ \alpha_2 \leq \alpha_1 \end{array}}{A \vdash \text{welltyped}(x = y)}$$

$x = y$   
let  $\text{ref}(\tau_1 \times \lambda_1) = \text{type}(\text{ecr}(x))$   
     $\text{ref}(\tau_2 \times \lambda_2) = \text{type}(\text{ecr}(y))$  in  
if  $\tau_1 \neq \tau_2$  then  $\text{cjoin}(\tau_1, \tau_2)$   
if  $\lambda_1 \neq \lambda_2$  then  $\text{cjoin}(\lambda_1, \lambda_2)$

## Advantages and disadvantages of this approach

- Advantages
  - type inference based: can derive an algorithm systematically from typing rules
  - fast
- Disadvantages
  - imprecise

## Summary

- Non-standard types can be used to compute interesting properties about programs
- Next lecture: Lackwit (reading on web page)
  - Using type inference to find bugs