

Types

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Some important dimensions in types

- When are types checked?
- How “completely” are types checked?
- When is it legal to do an assignment?
 - **Subtyping** is a clean mechanism for expressing this!
- When are types equal?

When to do “type checking”

- **Static type checking:** all checking at compile/link time
- **Dynamic type checking:** all checking at run time
- Most languages fall somewhere in between e.g., Java and Modula-3

Examples of type checking

- `int i;`
`int j;`
`i = j;` **Static**
- `char *p;`
`void *q;`
`p = q;` **Dynamic?**
- `int i;`
`char c;`
`c = i;` **Dynamic?**

How strong is the checking

- **Strongly-typed:** All expressions are checked (and guaranteed) to be type-consistent at compile or run time (**type-safe**).
 - Pascal, Modula-2, Modula-3, Java, ...
- **Weakly-typed:** Some expressions are not completely typechecked and unchecked type violations may happen at run time
 - C, C++, assembler

Strong and weak typing example

- `char *p;`
`void *q;`
`Check IsType(q, char*)`
`p = q;`
 - `int i;`
`char c;`
`Check IsType(i, char)`
`c = i;`
- Strong typing

Discussion: static versus dynamic typing

- Advantages of static
 - better performance
 - find errors early
 - more complete
- Disadvantages of static
 - less flexible (particularly for prototyping)
 - slower compilation

Discussion: strong versus weak typing

- Advantages of strong
 - more bugs found
 - may be faster
 - useful documentation in conjunction with static typing
- Disadvantages of strong
 - need to insert casts and checks for code to compile/run
 - device drivers
 - may be slower

What is legal?

- When is $x:T = y:U$ legal?
- When is $x:T \text{ op } y:U$ legal?
- Two important concepts:
 - type equality
 - subtyping

Type equality

- When are two types, T1 and T2, equal?
 - **Name equivalence**: when T1 and T2 have the same name. *Anonymous* types have unique “names”.
 - **Structural equivalence**: when T1 and T2 have the same structure.
- Structural equivalence: **Modula-3, Algol**
Name equivalence: **Modula-2, C, Java, C++, Ada**
Undefined: **Pascal**

Type equality examples

```
TYPE T1 = RECORD i: INTEGER; b: BOOLEAN; END;  
TYPE T2 = RECORD i: INTEGER; b: BOOLEAN; END;  
TYPE T3 = T2;
```

- $T1 = T2?$ $T1 = T3?$ $T2 = T3?$

A simple algorithm for structural equivalence

- $T1 = T2 \Rightarrow$
 - Replace all names in T1 and T2 with their expansion until T1 and T2 do not contain any type names
 - $T1 = T2$ if their expansions are identical

Structural equivalence example

```
TYPE T1 = RECORD i: INTEGER; b: T3; END;  
TYPE T2 = RECORD i: INTEGER; b: T4; END;  
TYPE T3 = RECORD x: BOOLEAN; END;  
TYPE T4 = RECORD x: BOOLEAN; END;
```

T1 \neq T2 expands into:

```
RECORD i: INTEGER; b: T3; END;  $\neq$   
RECORD i: INTEGER; b: T4; END;
```

Which further expands into

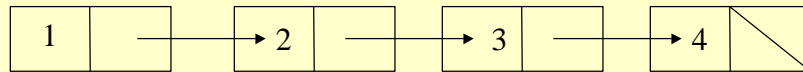
```
RECORD i: INTEGER; b: RECORD x: BOOLEAN; END; END;  $\neq$   
RECORD i: INTEGER; b: RECORD x: BOOLEAN; END; END;
```

which are identical

Structural equivalence--it ain't easy to do

```
TYPE T1 = RECORD          TYPE T2 = RECORD  
  value: INTEGER;        value: INTEGER;  
  next: REF T1;          next: REF T2;  
END                       END
```

The expansion is infinite for these types



Structural equivalence: new algorithm (simplified)

T1 = T2

- **FALSE** if T1.kind != T2.kind, else
- **TRUE** if T1 and T2 are identical or in *assume-equal*, else
- add (T1, T2) to *assume-equal*(T1, T2) and do a component-wise equality test on T1 and T2.
TRUE if all components have equal types

Example

```
TYPE T1 = RECORD   TYPE T2 = RECORD
  value: INTEGER;   value: INTEGER;
  next: REF T1;     next: REF T2;
END                END
```

assume-equal += (T1, T2)
compare(value: INTEGER, value: INTEGER)? returns **TRUE**
compare(next: REF T1, next: REF T2)?
assume-equal += (REF T1, REF T2)
compare(T1, T2)? returns **TRUE** since (T1,T2) in assume-equal

Advantages and disadvantages of name equivalence

- **Advantage**
 - Types with different names are treated differently
 - $\text{age}=[0..100] \neq \text{temperature}=[0..100]$
- **Disadvantages**
 - Not systematic:
 - Are $x: \text{int}; y: \text{int}$; of the same type?
 - Are $x: \text{struct } i: \text{integer end}; y: \text{struct } i: \text{integer end}$; of the same type?
 - $T = \text{struct } i: \text{integer end}; U=T$; Are $x: T; y: U$ of the same type?

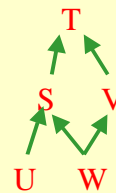
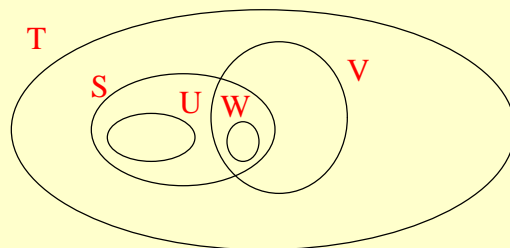
Type equivalence and distributed environments

```
Program Producer()  
a: ARRAY [1..1024] OF INTEGER  
send(Consumer, a)
```

```
Program Consumer()  
a: ARRAY [1..1024] OF INTEGER  
receive(a)
```

Subtyping

- Type S is a subtype of type T if every value of type S is also a value of type T
- Written as $S <: T$



Ways of thinking about subtyping

- Subtype may be used whenever the supertype is expected
 - e.g., if $x = i:\text{int}$ is legal then so is $x = i:[10..20]$
- Subtype has more stringent membership requirements than supertype
 - e.g., int versus $[10..20]$
- Subtype has fewer members than supertype
- widen: subtype \rightarrow supertype
narrow: supertype \rightarrow subtype

More examples of subtyping

Assignability

When is $b: B := a: A$ legal?

- Answer 1: $A <: B$ **Too restrictive?**
- Answer 2: $A <: B$ or $B <: A$ with some run-time type checking or conversions

```
VAR j: INTEGER; i: [10..20]      →   if j > 20 or j < 10 report_error  
i := j                          else i := cast(j)
```

When is type $A <: \text{type } B$

- Trivially if $A = B$
- Transitively if $A <: C$ and $C <: B$
- Subtyping between integers and subranges is easy: directly apply value inclusion
- How about sets?
A = SET of {red, blue}
B = SET of {red, blue, yellow}

Yes by value inclusion, but real languages often disallow this!

When is type $A <: \text{type } B$ (cont.)

- Arrays
A = ARRAY[1..10] OF INTEGER
B = ARRAY[11..20] OF INTEGER
 - $A <: B$ if arrays are sequences of values, and they have the same element type and same **length**
 - What if the arrays have different lengths?
 - What if the arrays have different element types?
 - **Performance considerations creep in!**
- Objects: by inheritance

Summary

- Many dimensions to a type system
 - Static or dynamic
 - Strong or weak
 - Structural or name equivalence
 - Type-checking rules
- Choices in the type system can affect performance

Next topic: Types in languages

- How are types incorporated into some common languages
- Reading:
 - *The Modula-3 type system*